Good evening! Thank you for coming.



This evening we will provide you with information on how we teach Mathematics at Moorlands and suggest ways that you can help your child at home using similar methods.



Maths at Moorlands. A focus on Concrete, Pictorial and Abstract approaches. (CPA) Karen Chapman and Justine Jackson Maths Leaders Moorlands Primary School

Why are we engaging parents?

BBC News Report 2006

69% of parents do not help children with their homework because...

Everything has changed since they were at school and they are not **confident** in the new methods.





Parent confidence and support



Lots of initiatives have been introduced, like 'Keeping up with the children,' 'Inspire workshops' and employing parental engagement coordinators in some schools.

Despite this, the situation worsened:

BBC News Report 2010

82% of parents feel unable to help pupils with their homework.

Lack of confidence.



The 'problem' with maths



"My dad thinks that the way **he** does maths is easier and better than **my** way but he doesn't understand my way and his way confuses me."

That's not the way we do it in school!

Pupil – Catford High School

In the Impact in Learning maths programme, children regularly talked about the **clash** between the maths learnt in school and what parents were showing them at home.



Why it is important to engage parents with the mathematical learning of their children?

Research evidence suggests that when parents are engaged in their children's learning, outcomes for children can be improved.

Research also highlights the fact that parents feel they need more support to understand the current curriculum content and how they can support their child with their learning at home.

Desforges, C. and Abouchaar, A. (2003); Goodall, J. and Vorhaus, J. (2011); The Education Endowment Foundation (2019); Sarjeant, S. (2021)



Agenda



- The theory behind the importance of CPA
- Using manipulatives to introduce the basics of a new concept and ways to replicate this at home.

• Transitioning between concrete, pictorial and abstract.



Concrete, Pictorial and Abstract Methods

Importance of CPA



In his research on the cognitive development of children (1966), Jerome Bruner proposed three ways of working to aid development:

- Enactive representation (using 'concrete' objects)
- Iconic representation (drawing images / pictures)
- Symbolic representation (abstract numbers)

"If we do not use concrete manipulations, then we can not understand mathematics. If we only use concrete manipulations, then we are not doing mathematics."

Gu (2015)

Concrete, Pictorial, Abstract



Children should work at the stage they need until ready to move on. Within a class children can be working on the same calculation but accessing it in different ways.



Using CPA methods



Today we aim to give you a quick insight into methods used at school for the 4 rules of number and how you could adapt those to work at home, with a focus on:

- Place value
- Addition and Subtraction
- Multiplication and Division
- Possible scope for a fractions evening later in the year if people would like that.



Place Value

(understanding the value of each digit and it's place in the number system)



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In KS1 children will work with base 10 resources when working with 2 digit numbers. This equipment helps them 'see' the 'ten-ness' of ten.







This moves on to Place Value Counters in KS2. (Year 3 / 4 / 5 / 6)





Pictorial Place Value counters

Draw the counters





Addition



Beginning to use formal written methods



• Formal column method will first of all be introduced using the visual of place value counters. This is so that children fully understand what is happening with the numbers when we exchange and carry over rather than just learning a process.



Can we exchange any counters?

ands Priman cross Addition- Column method Solve... 243 + 368 =Calculations Model 243 1 10 100 +3686 1 1 10 100 10 Key vocabulary: exchange

Can we exchange any counters?

Moving to pictorial



After lots of experience with the actual counters children should be able to draw the place value counters to help them solve a calculation, crossing out any counters that are to be exchanged.

Abstract



Children will naturally move away from drawing counters and carry out the calculation abstractly. Here it is clear the importance of being able to add single digits together with ease, including crossing the ten, as we looked at on the earlier slide. The highest numbers they will ever have to add is 9+9



Subtraction









Can we exchange any counters?



Key vocabulary: **exchange** *Can we exchange any counters?*

Pictorial and abstract



As with addition, after lots of experience with the actual counters children should be able to draw the place value counters to help them solve a calculation, crossing out any counters that are to be exchanged. This will then naturally move to working abstractly with the numbers.



Multiplication



Vocabulary

Multiplication	Division
Times Times by Multiply Multiply by Product Product of Lots of Groups of	Share between Share into Split Divide Group Split into



Language of multiplication



Multiplying 2 digit numbers by going of the second second

We often start on a bar model to show 6 lots of 23. This would be done first of all with no crossing over into the tens then we look at exchanging ones for tens.



3 x 6 = 20 x 6 =

Add the totals together



Place Value Grid

Tens	Ones	2	3	X	3	=
10 10	0 0	-	U		U	
10 10		1	x	3	=	
10 10	0 0 0	2	0	x	3	=
		•				



Pictorial with 2 digits





 Eventually, children will use an abstract method to calculate up to 4 digits by one digit including with multiple exchange.





Working abstractly





1. Multiply by the ones

2.Bring down a zero as we are multiplying by tens, the number needs to be ten times the size.

3. Add the 2 parts together.







KS2 Arithmetic Paper



Source: Q3, 6, 10, 20, 29 2023 KS2 Arithmetic Paper; Q16, 2017 KS2 Arithmetic Paper

KS2 Reasoning Paper (1)

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 All of these formal methods for multiplication, ultimately boil down to times table facts. Children who memorise times tables, move very swiftly through column work, as their working memory is not taken up with try to work out 7x8 for instance.



Which multiplication facts do White Rose students find tricky?



Source: https://www.cambridgemaths.org/Images/espresso_1_learning_and_assessing_times_tables.pdf



Do students need to memorise 144 facts?

1 × 1	1 × 2	1 × 3	1 × 4	1×5	1×6	1×7	1×8	1×9	1 × 10	1 × 11	1 × 12
2 × 1	2 × 2	2 × 3	2 × 4	2 × 5	2 × 6	2 × 7	2 × 8	2 × 9	2 × 10	2 × 11	2 × 12
3 × 1	3 × 2	3 × 3	3 × 4	3 × 5	3 × 6	3 × 7	3 × 8	3 × 9	3 × 10	3 × 11	3 × 12
4 × 1	4 × 2	4 × 3	4 × 4	4 × 5	4 × 6	4 × 7	4 × 8	4 × 9	4 × 10	4 × 11	4 × 12
5 × 1	5 × 2	5 × 3	5 × 4	5 × 5	5×6	5 × 7	5 × 8	5×9	5 × 10	5 × 11	5 × 12
6 × 1	6 × 2	6 × 3	6 × 4	6 × 5	6 × 6	6 × 7	6 × 8	6×9	6 × 10	6 × 11	6 × 12
7 × 1	7 × 2	7 × 3	7 × 4	7 × 5	7×6	7×7	7×8	7×9	7 × 10	7 × 11	7 × 12
8 × 1	8 × 2	8 × 3	8 × 4	8 × 5	8×6	8×7	8 × 8	8×9	8 × 10	8 × 11	8 × 12
9×1	9 × 2	9 × 3	9 × 4	9 × 5	9×6	9×7	9×8	9×9	9 × 10	9×11	9 × 12
10 × 1	10 × 2	10 × 3	10 × 4	10 × 5	10 × 6	10 × 7	10 × 8	10 × 9	10×10	10 × 11	10 × 12
11 × 1	11 × 2	11 × 3	11 × 4	11 × 5	11 × 6	11 × 7	11 × 8	11 × 9	11 × 10	11 × 11	11 × 12
12 × 1	12 × 2	12 × 3	12 × 4	12 × 5	12 × 6	12 × 7	12 × 8	12 × 9	12 × 10	12 × 11	12 × 12



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No – potentially, they only need to remember 45 facts. This is presuming children know the tens, and can connect the pattern of 12 x table being x ten plus a double and 11 x table being x 10 plus one more multiple.

Based on Kenny's travels to Shanghal

www.kangaroomaths.com



Division

















Step 1 Write out the multiples





Step 2 Work through as short division, how many 32s in 39

What multiple did I get to? 32. Write down the multiple and subtract.

This is really the same process as carrying over in short division, but we are writing it underneath.



Step 3 Bring down the next digit. SO we are now looking at 73. Repeat the steps. Work through as how many 32s in 73? 2

What multiple did I get to? 64. Write down the multiple and subtract.



32

64

96

123

Step 4 Bring down the next digit. SO we are now looking at 96. Repeat the steps. Work through as how many 32s in 96? 3

What multiple did I get to? 96. Write down the multiple and subtract. There are no remainders.







Thank you for listening. We hope we have given you a useful insight into using CPA approaches within Mathematics. If you have any questions please don't hesitate to ask.